

ADA PINPOINT TOPIC PACKS

(1) Simultaneous Equations (8 Qns)

(2) Simultaneous Equations with a Quadratic (2 Qns)

(3) Solving Simultaneous Equations Graphically (2 Qns)

50_to_100_Percent_Pinpoint_AI_Pack

Time Allocation = 45mins , Max = 40 Marks

Calculated Grade Boundaries:

Grade	Marks
5-	3
5	6
5+	8
6-	11
6	14
6+	16
7-	19
7	22
7+	24
8-	27
8	30
8+	32
9-	35
9	38
9+	40

Question 1 (AO1): 50% of students got this right (3 marks)

2 Solve the simultaneous equations

$$\begin{aligned}3x + y &= -4 \\3x - 4y &= 6\end{aligned}$$

(Total for Question 2 is 3 marks)

Question 2 (AO2): (No Calc) 50% of students got this right (4 marks)

20. Solve the simultaneous equations

$$5x + 2y = 11$$

$$4x - 3y = 18$$

$x =$

$y =$

(Total for Question 20 is 4 marks)

Question 3 (AO3): 48% of students got this right (4 marks)

15. A cinema sells adult tickets and child tickets.

The total cost of 3 adult tickets and 1 child ticket is £30.

The total cost of 1 adult ticket and 3 child tickets is £22.

Work out the cost of an adult ticket and the cost of a child ticket.

adult ticket £.....

child ticket £.....

(Total for Question 15 is 4 marks)

Question 4 (AO2): (No Calc) 43% of students got this right (4 marks)

15. Solve the simultaneous equations

$$3x + 4y = 5$$

$$2x - 3y = 9$$

$$x = \dots\dots\dots$$

$$y = \dots\dots\dots$$

(Total for Question 15 is 4 marks)

Question 5 (AO2): (No Calc) 34% of students got this right (3 marks)

18. Solve the simultaneous equations

$$4x + y = 25$$

$$x - 3y = 16$$

$x =$

$y =$

Question 6 (AO2): (No Calc) 33% of students got this right (3 marks)

19. Solve the simultaneous equations

$$4x + y = 10$$

$$2x - 3y = 19$$

$$x = \dots\dots\dots$$

$$y = \dots\dots\dots$$

(Total 3 marks)

Question 7 (AO2): 32% of students got this right (4 marks)

18. Solve the equations

$$3x + 5y = 19$$

$$4x - 2y = -18$$

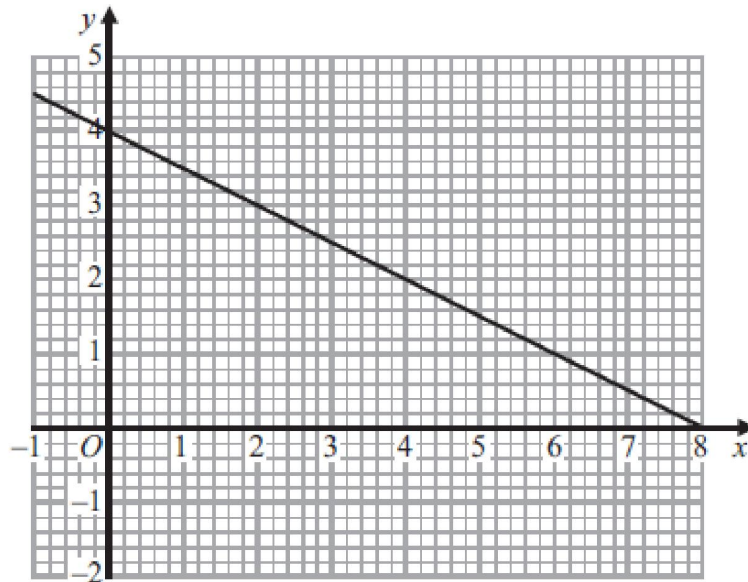
$x = \dots\dots\dots$

$y = \dots\dots\dots$

(Total 4 marks)

Question 8 (AO1): (No Calc) 28% of students got this right (1 marks)

13.



The graph of the straight line $x + 2y = 8$ is shown on the grid.

(a) On the grid, draw the graph of $y = \frac{x}{2} - 1$

RETEST QUESTION

(b) Use the graphs to find estimates for the solution of

$$x + 2y = 8$$

$$y = \frac{x}{2} - 1$$

$$x = \dots\dots\dots y = \dots\dots\dots$$

(1)**(Total 4 marks)**

Question 9 (AO3): (No Calc) 15% of students got this right (4 marks)

17 Solve

$$2x + 3y = \frac{2}{3}$$

$$3x - 4y = 18$$

$x = \dots\dots\dots$

$y = \dots\dots\dots$

(Total for Question 17 is 4 marks)

Question 10 (AO1): (No Calc) 11% of students got this right (5 marks)

20 Solve algebraically

$$x^2 + y^2 = 2$$

$$y - 2x = -1$$

.....
(Total for Question 20 is 5 marks)

Question 11 (AO1): (No Calc) 11% of students got this right (5 marks)

20 Solve algebraically the simultaneous equations

$$\begin{aligned}x^2 + y^2 &= 25 \\y - 3x &= 13\end{aligned}$$

.....
(Total for Question 20 is 5 marks)

Answers to Qn 1 (AO1): 50% of students got this right

Question 2 (Total 3 marks)

Part	Working or answer an examiner might expect to see	Mark	Notes
	$3x - 3x = 0$, $y - -4y = 5y$, $4 - 6 = -10$ $5y = -10$	M1	This mark is given for a method to eliminate one variable
	$y = -2$ $3x - 2 = -4$ or $3x + 8 = 6$	M1	This mark is given for substituting one found value in one of the equations
	$3x = -2$ $x = -\frac{2}{3}$, ($y = -2$)	A1	This mark is given for a correct pair of answers only

Answers to Qn 2 (AO2): (No Calc) 50% of students got this right

20 Solve the simultaneous equations

$$\begin{aligned} 5x + 2y &= 11 & \textcircled{1} \\ 4x - 3y &= 18 & \textcircled{2} \end{aligned}$$

$$\begin{aligned} 15x + 6y &= 33 & \textcircled{1} \times 3 \\ 8x - 6y &= 36 & \textcircled{2} \times 2 \end{aligned}$$

$$\begin{array}{r} \textcircled{1} \\ + \\ \textcircled{2} \\ \hline \end{array} \downarrow$$

$$23x = 69$$

$$x = 3$$

Sub $x = 3$ into $\textcircled{1}$

$$5 \times 3 + 2y = 11$$

$$15 + 2y = 11$$

$$2y = -4$$

$$y = -2$$

Answers to Qn 3 (AO3): 48% of students got this right

15 A cinema sells adult tickets and child tickets.

The total cost of 3 adult tickets and 1 child ticket is £30

The total cost of 1 adult ticket and 3 child tickets is £22

Work out the cost of an adult ticket and the cost of a child ticket.

$$\begin{array}{r} 3a + c = 30 \quad \times 3 \\ a + 3c = 22 \quad \times 1 \end{array}$$

$$9a + 3c = 90$$

$$\underline{-} a + \underline{-} 3c = \underline{-} 22$$

$$8a = 68$$

$$a = 8.5 \quad (\pounds 8.50)$$

$$8.5 + 3c = 22$$

$$3c = 13.5$$

$$c = 4.5 \quad (\pounds 4.50)$$

Answers to Qn 4 (AO2): (No Calc) 43% of students got this right

15 Solve the simultaneous equations

$$3x + 4y = 5 \quad \times 2$$

$$2x - 3y = 9 \quad \times 3$$

$$(1) \quad 6x + 8y = 10$$

$$(2) \quad 6x - 9y = 27$$

$$(1) - (2)$$

$$0 + 17y = -17$$

$$17y = -17$$

$$\underline{\underline{y = -1}}$$

Sub in $y = -1$

$$2x - 3(-1) = 9$$

$$2x + 3 = 9$$

$$2x = 6$$

$$\underline{\underline{x = 3}}$$

Answers to Qn 5 (AO2): (No Calc) 34% of students got this right

18 Solve the simultaneous equations

$$\textcircled{1} \quad 4x + y = 25$$

$$\textcircled{2} \quad x - 3y = 16$$

$$\textcircled{1} \times 3 : \quad 12x + 3y = 75$$

$$\textcircled{2} \quad : \quad x - 3y = 16$$

$$\textcircled{1} + \textcircled{2} : \quad 13x = 91$$

$$x = \underline{7}$$

sub into $\textcircled{1}$: $4 \times 7 + y = 25$

$$28 + y = 25$$

$$y = \underline{-3}$$

$$x = \underline{7}$$

$$y = \underline{-3}$$

Answers to Qn 6 (AO2): (No Calc) 33% of students got this right

19. Solve the simultaneous equations

$$\begin{aligned} \textcircled{1} \quad & 4x + y = 10 \\ \textcircled{2} \quad & 2x - 3y = 19 \end{aligned}$$

$$\begin{array}{r} \textcircled{1} \times 3 \Rightarrow 12x + 3y = 30 \\ \textcircled{2} \Rightarrow 2x - 3y = 19 \quad + \\ \hline 14x \qquad \qquad = 49 \\ x = \frac{49}{14} = \frac{7}{2} = 3.5 \end{array}$$

sub into $\textcircled{1}$

$$4(3.5) + y = 10$$

$$\begin{array}{r} 14 + y = 10 \\ -14 \quad y \quad -14 \end{array}$$

$$y = -4$$

$$x = \underline{\underline{3.5}}$$

$$y = \underline{\underline{-4}}$$

Answers to Qn 7 (AO2): 32% of students got this right

18. Solve the equations

$$\begin{array}{r}
 3x + 5y = 19 \\
 4x - 2y = -18 \\
 \hline
 12x + 20y = 76 \quad \dots \quad \textcircled{1} \\
 - \quad 12x - 6y = -54 \quad \dots \quad \textcircled{2} \\
 \hline
 \end{array}$$

① - ②

$$26y = 130$$

$$\underline{y = 5}$$

subs. $y = 5$ into $3x + 5y = 19$

$$3x = 19 - 25$$

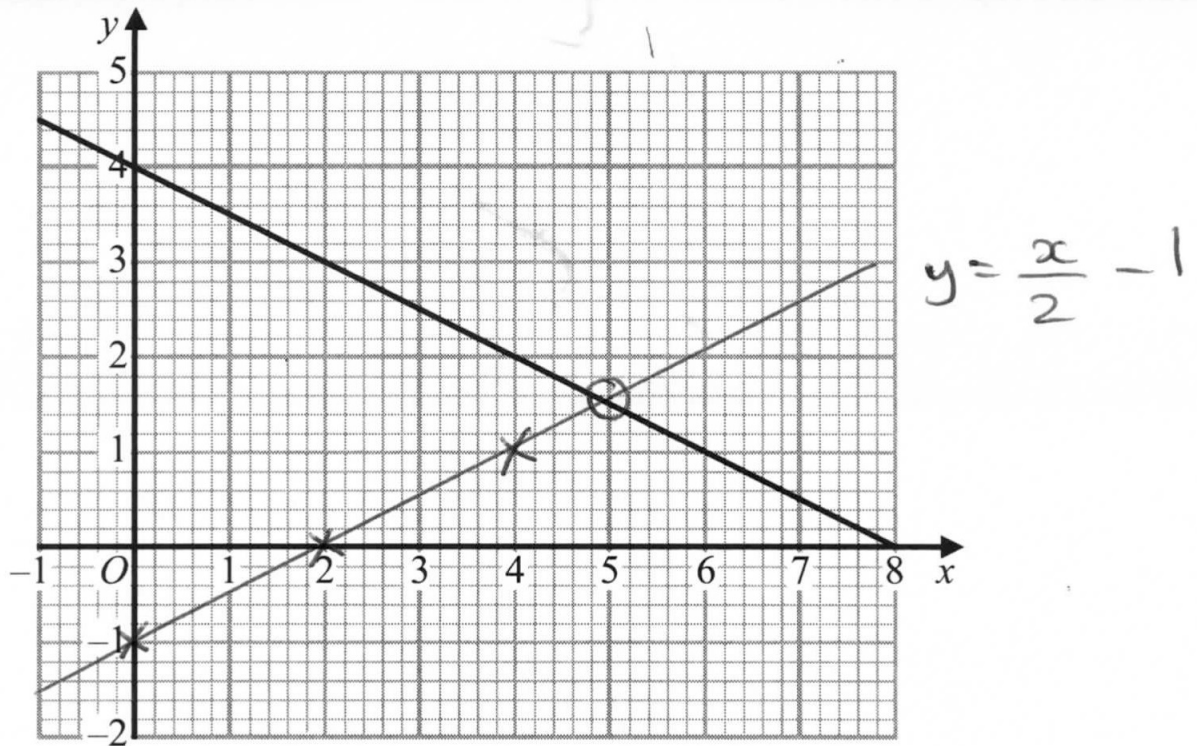
$$3x = -6$$

$$\underline{x = -2}$$

$$\begin{array}{l}
 x = \dots - 2 \dots \\
 y = \dots 5 \dots
 \end{array}$$

Answers to Qn 8 (AO1): (No Calc) 28% of students got this right

13.



The graph of the straight line $x + 2y = 8$ is shown on the grid.

(a) On the grid, draw the graph of $y = \frac{x}{2} - 1$

(3)

(b) Use the graphs to find estimates for the solution of

$$x + 2y = 8$$

$$y = \frac{x}{2} - 1$$

$$x = \dots 5 \dots y = \dots 1.6 \dots$$

(1)

Answers to Qn 9 (AO3): (No Calc) 15% of students got this right

17			$x = 1\frac{3}{5}$ $y = 3\frac{1}{3}$	4	<p>M1 for a correct process to eliminate either variable (condone one arithmetic error) or to rearrange and substitute for elimination</p> <p>A1 cao for either x or y</p> <p>M1 (dep on M1) for correct substitution of found value into one of the equation or appropriate method after starting again (condone one arithmetic error)</p> <p>A1 cao</p>
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Answers to Qn 10 (AO1): (No Calc) 11% of students got this right

20 Solve algebraically

$$x^2 + y^2 = 2 \quad (1)$$

$$y - 2x = -1 \quad y = 2x - 1 \quad (2)$$

$$\begin{aligned} \text{Sub (2) into (1): } x^2 + (2x - 1)^2 &= 2 \\ x^2 + 4x^2 - 4x + 2 &= 2 \\ 5x^2 - 4x &= 0 \\ x(5x - 4) &= 0 \end{aligned}$$

$$\text{So } x = 0 \quad \text{or } x = \frac{4}{5}$$

$$\text{And } y = -1 \quad \text{or } y = 2 \times \frac{4}{5} - 1 = \frac{3}{5}$$

.....
(Total for Question 20 is 5 marks)

Answers to Qn 11 (AO1): (No Calc) 11% of students got this right

Question 20 (Total 4 marks)

Part	Working or answer an examiner might expect to see	Mark	Notes
	$y - 3x = 13$, so $y = 3x + 13$ $x^2 + (3x + 13)^2 = 25$	M1	This mark is given for the substitution of $y = 3x + 13$ into $x^2 + y^2 = 25$
	$x^2 + 9x^2 + 39x + 39x + 169 = 25$	M1	This mark is given for the expansion of $x^2 + (3x + 13)^2 = 25$
	$10x^2 + 78x + 144 = 0$	M1	This mark is given for forming a quadratic equation equal to zero
	$2(5x^2 + 39x + 72) = 0$ $2(5x + 24)(x + 3) = 0$	M1	This mark is given for a method to solve the quadratic equation
	$x = -3$, $y = 4$ $x = -\frac{24}{5}$, $y = -\frac{7}{5}$	A1	This mark is given for a pair of correct solutions only